Financial derivatives 2014/2015 "Fundamentals" part of the oral exam

- Definitions of a Wiener process, a Brownian motion and a geometrical Brownian motion.
- Itō lemma: statement of the one-dimensional Itō lemma, its intuitive proof, application finding explicit solution to $dS = \mu S dt + \sigma S dw$ where μ, σ are constants and w is a Wiener process.
- Derivation of the Black-Scholes partial differential equation using Black-Scholes approach.
- Historical volatility (definition, derivation of the estimator) and implied volatility (definition, existence and uniqueness the Black-Scholes formula is provided).
- Derivation of the delta for call and put options in the Black-Scholes framework (the Black-Scholes formula is provided). The concept of delta hedging.
- Numerical methods for the heat equation derivation of implicit and explicit schemes.