

Lineárne a kvázilineárne PDR prvého rádu

Nájdite všeobecné riešenie nasledovných rovníc (v príkladoch 16-18 je hľadaná funkcia $u = u(x, y, z)$, inde $z = z(x, y)$):

1. $y \frac{\partial z}{\partial x} + x \frac{\partial z}{\partial y} = x - y$
2. $e^x \frac{\partial z}{\partial x} + y^2 \frac{\partial z}{\partial y} = ye^x$
3. $2x \frac{\partial z}{\partial x} + (y - x) \frac{\partial z}{\partial y} - x^2 = 0$
4. $xy \frac{\partial z}{\partial x} - x^2 \frac{\partial z}{\partial y} = yz$
5. $x \frac{\partial z}{\partial x} + 2y \frac{\partial z}{\partial y} = x^2 y + z$
6. $(x^2 + y^2) \frac{\partial z}{\partial x} + 2xy \frac{\partial z}{\partial y} + z^2 = 0$
7. $2y^4 \frac{\partial z}{\partial x} - xy \frac{\partial z}{\partial y} = x\sqrt{z^2 + 1}$
8. $x^2 z \frac{\partial z}{\partial x} + y^2 z \frac{\partial z}{\partial y} = x + y$
9. $yz \frac{\partial z}{\partial x} - xz \frac{\partial z}{\partial y} = e^z$
10. $(z - y)^2 \frac{\partial z}{\partial x} + xz \frac{\partial z}{\partial y} = xy$
11. $xy \frac{\partial z}{\partial x} + (x - 2z) \frac{\partial z}{\partial y} = yz$
12. $y \frac{\partial z}{\partial x} + z \frac{\partial z}{\partial y} = \frac{y}{x}$
13. $\sin^2 x \frac{\partial z}{\partial x} + \operatorname{tg} z \frac{\partial z}{\partial y} = \cos^2 z$
14. $(x + z) \frac{\partial z}{\partial x} + (y + z) \frac{\partial z}{\partial y} = x + y$
15. $(xz + y) \frac{\partial z}{\partial x} + (x + yz) \frac{\partial z}{\partial y} = 1 - z^2$
16. $(y + z) \frac{\partial u}{\partial x} + (z + x) \frac{\partial u}{\partial y} + (x + y) \frac{\partial u}{\partial z} = u$
17. $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + (z + u) \frac{\partial u}{\partial z} = xy$
18. $(u - x) \frac{\partial u}{\partial x} + (u - y) \frac{\partial u}{\partial y} - z \frac{\partial u}{\partial z} = x + y$
19. $y^2 \frac{\partial z}{\partial x} + xy \frac{\partial z}{\partial y} = x$
20. $x \frac{\partial z}{\partial x} - 2y \frac{\partial z}{\partial y} = x^2 + y^2$