

- Viacrozmerné normálne rozdelenie

$$f(x) = (2\pi)^{-p/2} (\det(\Sigma))^{-1/2} \exp\{-1/2(x - \mu)^T \Sigma^{-1} (x - \mu)\}$$

$$\varphi_X(t) = \exp\{it^T \mu - 1/2t^T \Sigma t\}$$

- Wishartovo rozdelenie $M = X^T X \sim W_p(\Sigma, n)$, $X^T = (X_1, \dots, X_n)$, X_1, \dots, X_n z $N_p(0, \Sigma)$.

- Podmienené rozdelenia

– Nech $X = (X_1, X_2)^T \sim N_p(\mu, \Sigma)$, kde $X_1 \in \mathbb{R}^r$ a $X_2 \in \mathbb{R}^{p-r}$.

$$(X_2 | X_1 = x_1) \sim N_{p-r}(\mu_2 + \Sigma_{21} \Sigma_{11}^{-1} (x_1 - \mu_1), \Sigma_{22} - \Sigma_{21} \Sigma_{11}^{-1} \Sigma_{12}).$$

– $X_1 \sim N_r(\mu_1, \Sigma_{11})$ a $(X_2 | X_1 = x_1) \sim N_{p-r}(Ax_1 + b, M) \Rightarrow X = (X_1, X_2)^T \sim N_p(\mu, \Sigma)$, kde $\mu = (\mu_1, A\mu_1 + b)^T$ a

$$\Sigma = \begin{pmatrix} \Sigma_{11} & \Sigma_{11} A^T \\ A \Sigma_{11} & M + A \Sigma_{11} A^T \end{pmatrix}.$$

- Hotellingovo rozdelenie $\alpha = m d^T M^{-1} d \sim T^2(p, m)$, kde $d \sim N(0, I_p)$, $M \sim W_p(I, m)$ nez.